

## Solving Equations by Factoring:

allows us to solve equations of degree 2 and higher using skills we've previously learned

Steps:

1. make sure the equation is equal to zero; if not, make it equal to zero
2. factor the equation like we have done previously (GCF, Reverse FOIL, slide & divide)
3. set each factor (or set of parentheses) equal to zero
4. solve each equation for x

## Example 1:

Solve by factoring.

$$2x^2 + 18x + 28 = 0$$

Step 1: Equal to 0? = yes

Step 2: Factor. Is there a GCF? - yes  $x^2 \cdot 9x + 14 = 0$   
Factor. Since there is just  $(x+7)(x+2) = 0$   
 $x^2$ , find the factors of last that add to be the middle.

Step 3: Set each parentheses equal to 0.  $x+7=0$   $x+2=0$

Step 4: Solve.

$$\text{roots } x = -7 \quad x = -2$$

## Example 2:

Solve by factoring.

$$x^2 - 36 = 5x$$

Step 1: Equal to 0 - no.

$$x^2 - 5x - 36 = 0$$

Step 2: Factor. No GCF.

No coefficient on  $x^2$   
so factors of last that  
add to be middle.

$$(x-9)(x+4) = 0$$

Step 3: Set each parentheses = to 0  $x-9=0$   $x+4=0$

Step 4: Solve.

$$\text{Roots } x = 9 \quad x = -4$$

## Example 3:

Solve by factoring.

$$2x^2 - 5x - 12 = 0$$

Step 1 - done.

Step 2 - no GCF.

Factor with slide & divide.  $(x-4)(2x+3) = 0$

Step 3 - set each parentheses = 0

Step 4 - solve.

$$\text{roots } x = 4 \quad x = -\frac{3}{2} \text{ or } -1.5$$

## Example 5:

Solve by factoring.

$$a^2 - 24a = -144$$

Step 1 - set = to 0

Step 2 - factor - no GCF

factors of last that add up  
to middle

Step 3 - set each parentheses

Step 4 - solve

Since roots are the same, the vertex is also the root.

$$a^2 - 24a + 144 = 0$$

$$(a-12)(a-12) = 0$$

$$a-12=0 \quad a-12=0$$

$$a=12 \quad a=12$$

## Example 6:

Solve by factoring.

$$3x^2 - 7x - 20 = 0$$

Step 1 - done

Step 2 - factor. No GCF,  
so slide and divide.

Step 3 - set each parentheses = 0

Step 4 - solve.

$$-60 \div 5 = -12$$

$$(x-12)(x+5) = 0$$

$$(x-4)(3x+5) = 0$$

$$x-4=0 \quad 3x+5=0$$

$$x=4 \quad \frac{3x}{3} = -\frac{5}{3}$$

$$x = -\frac{5}{3}$$