

Problem of the Day: Solve the equation by factoring.
 $3x^2 + 4 = -13x$

Plan for the Day:

Notes on solving quadratics with square root method

More practice with square root method

Homework Week 23 is due tomorrow

Objective: We will be able to solve quadratics using the square root method.

Today is National Chocolate Mousse Day!!



Solve the equation by factoring.

$$x^2 + 7x + 20 = 0$$

$$\begin{array}{r} 20 \overline{) 7} \\ \underline{-14} \\ 20 \\ \underline{-20} \\ 0 \end{array}$$

Since not all quadratic equation are factorable, you need other methods.

One such method is the square root method.

This method only works for quadratics that have the form $ax^2 + c = \#$.

$$a(x-h)^2 + k$$

To solve a quadratic in the form $ax^2 + c = \#$,

1. move c to the other side of the equation
2. divide by a
 - if the result is positive, go to step 3
 - if the result is negative, then the solution is no real roots
3. square root each side of the equation
4. The solutions will be a positive and negative version of the square root.

Example 1: Solve using the square root method.

$$4x^2 + 3 = 39$$

$$\begin{array}{r} -3 \quad -3 \\ \hline 4x^2 = 36 \\ \hline 4 \quad 4 \end{array}$$

$$\sqrt{x^2} = \sqrt{9}$$

$$x = 3 \text{ and } x = -3$$

$$x = \pm 3$$

$$3^2 = 9$$

$$(-3)^2 = 9$$

Example 2: Solve using the square root method.

$$100x^2 + 10 = 19$$

$$\begin{array}{r} -10 \quad -10 \\ \hline 100x^2 = 9 \\ \hline 100 \quad 100 \end{array}$$

$$\sqrt{x^2} = \sqrt{\frac{9}{100}} = \frac{\sqrt{9}}{\sqrt{100}}$$

$$x = \pm \frac{3}{10}$$

Example 3: Solve using the square root method.

$$2x^2 + 6 = -12$$

$$\begin{array}{r} -6 \quad -6 \\ \hline 2x^2 = -18 \end{array}$$

$$\begin{array}{r} \frac{2}{2} \quad \frac{2}{2} \\ \hline x^2 = -9 \end{array}$$

$$x^2 = -9$$

no real roots

$$\begin{array}{l} (-3)^2 = 9 \\ 3^2 = 9 \end{array}$$

Example 4: Solve using the square root method.

$$-1 - 8x^2 = -161$$

$$\begin{array}{r} +1 \quad +1 \\ \hline -8x^2 = -160 \end{array}$$

$$\begin{array}{r} \frac{-8}{-8} \quad \frac{-160}{-8} \\ \hline x^2 = 20 \end{array}$$

$$\sqrt{x^2} = \sqrt{20}$$

$$x = \pm 2\sqrt{5} \text{ or } \pm 4.5$$

Example 5: Solve using the square root method.

$$5x^2 - 10 = -10$$

$$\begin{array}{r} +10 \quad +10 \\ \hline 5x^2 = 0 \end{array}$$

$$\begin{array}{r} \frac{5}{5} \quad \frac{5}{5} \\ \hline x^2 = 0 \end{array}$$

$$\sqrt{x^2} = \sqrt{0}$$

$$x = 0 \text{ origin is vertex}$$

Example 6: Solve using the square root method.

$$10x^2 + 6 = 366$$

$$\begin{array}{r} -6 \quad -6 \\ \hline 10x^2 = 360 \end{array}$$

$$\begin{array}{r} \frac{10}{10} \quad \frac{360}{10} \\ \hline x^2 = 36 \end{array}$$

$$\sqrt{x^2} = \sqrt{36}$$

$$x = \pm 6$$